

Induced anisotropies in a ferromagnet coupled to a polycrystalline antiferromagnetJyotirmoy Saha,¹ Kevin Garello,^{2,3,4} B. Viala,^{2,3} A. Marty,¹ and N. Vukadinovic⁵¹CEA, INAC/SP2M/NM, 38054 Grenoble, Cedex 9, France²CEA, LETI, MINATEC, 38054 Grenoble, France³SPINTEC, CEA, CNRS, INPG, CEA/INAC, UJF, 38054 Grenoble, France⁴XLIM, CNRS, 87060 Limoges, France⁵Dassault Aviation, 92552 Saint-Cloud, France

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The effect of thermal activation of a polycrystalline antiferromagnet (AF) coupled to a ferromagnet (FM) on the unidirectional anisotropy responsible for positive shift of the resonant frequency (f_R) of the FM is presented. Hysteresis loops and ferromagnetic resonance plots of $\text{Co}_{35}\text{Fe}_{65}/\text{Ni}_{50}\text{Mn}_{50}$ are evaluated and matched with those obtained from experiments. The contribution of the AF magnetic structure to f_R is highlighted. An inverse relation between f_R and AF grain size is predicted.

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I. INTRODUCTION

When a ferromagnet (FM) is coupled to a polycrystalline antiferromagnet (AF), the magnetocrystalline anisotropy of the AF induces various forms of anisotropies in the FM mediated by uncompensated spins^{1,2} at the AF-FM interface (henceforth, interface). The tuning of these anisotropies has been an important endeavor for industries in the development of spin valve and microwave devices.³ The two basic yet cardinal experimental outcomes that quantify these anisotropies are: (1) hysteresis loops (HLs) yielding exchange bias (H_E) and enhanced coercivity (H_{EC}) and (2) ferromagnetic resonance (FMR) plots yielding the resonant frequency (f_R). The important distinction between these two classes of experiments is that H_E is a measure of the induced unidirectional anisotropy (henceforth, UA) in the FM as the FM switches between the two magnetic states whereas f_R is a perturbative measure of the UA about the ground state of the system.^{4,5} In either case thermal activation of the AF primarily regulates the UA albeit in disparate ways. A strong research focus has been to formulate a canonical connection between these two classes of UA but an overall consensus in this matter is still at large. To achieve this, most (prior) endeavors have estimated f_R utilizing information from experimental HLs and tailoring techniques using the single domain particle (Kittel) approach.^{4,6,7} These techniques are system specific and moreover do not present a treatment of the thermal activation of the large AF degrees of freedom. Further progress in this field necessitates a theoretical model that can independently evaluate the FMR profiles and HLs in a multitude of systems based on system (material) attributes. An earlier work reported a model that evaluates HLs and also studied this aspect of AF/FM systems extensively.⁸ Utilizing building blocks of this model, in this paper we present a technique to evaluate the FMR response of AF/FM systems. Here, we investigate two metallic systems that are of current technological relevance: (1) $\text{Co}_{35}\text{Fe}_{65}/\text{Ni}_{50}\text{Mn}_{50}$ (henceforth CoFe/NiMn) and (2) $\text{Ni}_{80}\text{Fe}_{20}/\text{Ni}_{50}\text{Mn}_{50}$ (henceforth Py/NiMn). Experiments are carried out for the CoFe/NiMn system and the model predictions for the Py/NiMn system are compared to existing reports.

II. EXPERIMENTAL DETAILS AND MATERIAL CHARACTERISTICS

The experimental magnetic bilayer structure consists of: $\text{Si}(525 \mu\text{m})/\text{SiO}_2(2 \mu\text{m})/\text{Ru}(5 \text{ nm})/\text{Ni}_{50}\text{Mn}_{50}(t_{\text{AF}} = 50 \text{ nm})/\text{Co}_{35}\text{Fe}_{65}(t_{\text{FM}})/\text{Ru}(5 \text{ nm})$ with $t_{\text{FM}} = 10 \text{ nm}, 15 \text{ nm}, 20 \text{ nm}$ and 25 nm ; where, t_{AF} (t_{FM}) is the AF (FM) thickness. The composite system has an area of $4 \times 4 \text{ mm}^2$. They are grown by RF-magnetron sputtering on thermally oxidized silicon. The deposition is done at room temperature in the absence of a magnetic field with a base pressure of $9 \times 10^{-8} \text{ mbar}$ and an Argon plasma pressure of $2 \times 10^{-3} \text{ mbar}$. Following deposition, the composite system is annealed in vacuum for an hour at 573 K in an applied field of 500 Oe to induce the unidirectional anisotropy in the system. The HLs are obtained using a vibrating sample magnetometer (VSM). Post annealing, the $\text{Co}_{35}\text{Fe}_{65}$ free layer has a saturation magnetization (M_S) of $1.87 \times 10^3 \text{ emu/cc}$ and the easy axis loop yields a coercivity of 17.5 Oe. The complex permeability spectra of the samples are measured from 0.1–10 GHz using a refined single-loop coil technique, based on the model of Bekker *et al.*⁹ The small amplitude radio frequency (rf) field is applied perpendicular to the field-cooling direction. The magnetic characteristics of CoFe (Py) used in the model are: $M_S = 1.8 \times 10^3 \text{ emu/cc}$ ($8.6 \times 10^2 \text{ emu/cc}$),^{8,10} uniaxial magnetocrystalline anisotropy ($K_{\text{FM}} = 1.57 \times 10^4 \text{ ergs/cc}$ ($4.3 \times 10^3 \text{ ergs/cc}$),^{8,10,11} Curie temperature ($T_C = 1299 \text{ K}$ (850 K),^{8,12} exchange constant ($A_{\text{exchange}} = 1.75 \times 10^{-6} \text{ ergs/cm}$ ($1.0 \times 10^{-6} \text{ ergs/cm}$),^{8,10} and damping parameter ($\alpha = 0.005$ (0.02)).^{8,10} The magnetic structure of NiMn incorporates a biaxial in-plane (easy plane) magnetocrystalline anisotropy (K_{AF}) of $5 \times 10^5 \text{ ergs/cc}$ in the (001) plane and an out-of-plane anisotropy of $5.8 \times 10^6 \text{ ergs/cc}$ and grows with the $\langle 111 \rangle$ texturing.¹³ The interfacial AF moments are restricted to this (easy) plane due to the absence of an energy scale that can match the out-of-plane anisotropy. The density of lattice sites (D_{lattice}) at the interface is $8.64 \times 10^{14} \text{ sites/cm}^2$ and the Néel temperature (T_N) of NiMn is 1070 K.¹³

III. THEORETICAL MODEL

In the model the FM layer is treated micromagnetically, a thin sample of FM is discretized into uniformly magnetized

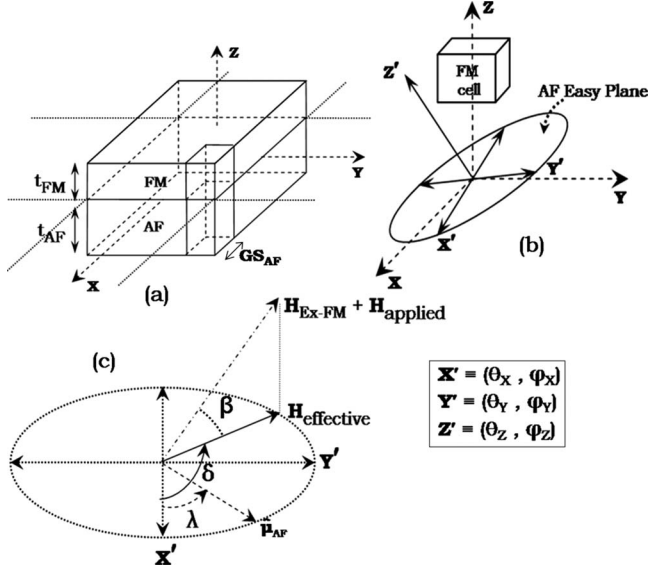


FIG. 1. (a) Discretization of the AF and FM layers; (b) easy plane (001) of an AF grain with respect to its texturing $\langle 111 \rangle$, the X', Y', Z' axes are denoted by their spherical angles with respect to the X - Y - Z coordinate system, $\theta_Z = 54.7^\circ$; and (c) easy plane of an AF grain. $H_{\text{ex-FM}}$ is the exchange field on an AF grain due to the interaction with the FM cell [Eq. (1)].

rectangular parallelepipeds with a square interface that couples with an AF grain [Fig. 1(a)]. The AF grains are considered noninteracting. The coupling energy¹⁴ between each FM cell and the corresponding AF grain is

$$E_{\text{AF-FM}} = -J_{\text{int}} \tilde{N} \hat{\mu}_{\text{AF}} \cdot \hat{\mu}_{\text{FM}}, \quad (1)$$

where, $J_{\text{int}} = 6\sqrt{J_{\text{FM}} J_{\text{AF}}} / (N_{\text{int}} + 1)$; \tilde{N} is the net imbalance of the moment direction at the interface due to uncompensated spins; $\hat{\mu}_{\text{AF}}$ is the direction of the net AF moment ($\tilde{N} \mu_{\text{AF}}$) induced at the interface; and $\mu_{\text{FM}} = M_S V_{\text{FM}} \hat{\mu}_{\text{FM}}$, where V_{FM} is the volume of the FM cell. J_{FM} and J_{AF} are estimated in the mean field sense from the knowledge of T_C and T_N . N_{int} is the number of interdiffused interfacial monolayers (chosen to be 1) which corresponds to an AF-FM interface thickness of 4.2 Å.¹³ The time evolution of each FM degree of freedom is evaluated by numerically integrating the Landau-Lifshitz-Gilbert equation: $\frac{d\mu_{\text{FM}}}{dt} = -\left(\frac{\gamma}{1+\alpha^2}\right) \mu_{\text{FM}} \times \mathbf{H} - \left(\frac{\alpha\gamma}{1+\alpha^2}\right) \hat{\mu}_{\text{FM}} \times (\mu_{\text{FM}} \times \mathbf{H})$; where γ is the gyromagnetic ratio of the free electron and \mathbf{H} is the net field experienced by a FM cell.¹⁵

The energy (E_{AF}) of each AF grain of volume V_{AF} is considered within the framework of a uniform rotation model [Fig. 1(c)]

$$E_{\text{AF}} = 2K_{\text{AF}} V_{\text{AF}} \left[\frac{\sin^2 2\lambda}{8} - h \cos(\delta - \lambda) \right], \quad (2)$$

where $h \sim \frac{J_{\text{int}} \tilde{N}}{2K_{\text{AF}} V_{\text{AF}}} \cos(\beta)$. The time evolution of $\tilde{N} \mu_{\text{AF}}$ of each AF grain is determined by its ability to switch over energy barriers (E_{Barrier}) to a lower energy state.⁸

The switching occurs when the Néel-Arrhenius condition is satisfied

$$E_{\text{Thermal}} \geq E_{\text{Barrier}} \quad (3)$$

where $E_{\text{Thermal}} = k_B T \ln(2f_0 t_{\text{SW}})$; where, k_B is the Boltzmann constant, $f_0 (=1 \text{ GHz})$ is the attempt frequency, t_{SW} is the time available for the AF grain to switch and is estimated from typical VSM sweep rates. To incorporate the polycrystalline nature of the AF, φ_Z , and φ_X [Fig. 1(b)] are uniformly distributed in the range $[0, 2\pi]$. $\hat{\mu}_{\text{FM}}$ and λ [Fig. 1(c)] are initialized randomly. To set the UA, a field of 1000 Oe along X (Fig. 1) is selected and a temperature of 1000 K is chosen. To compute the HL, the applied field is swept along the $\pm X$ direction. To evaluate the frequency response of the system, the zero-applied-field equilibrium value of the average FM magnetization (M_0) is noted. An impulse¹⁶ along the Y direction (Fig. 1) is applied and the system is then allowed to relax back to M_0 . As the system relaxes, the quantity $M_0 - M(t)$ is recorded where $M(t)$ is the average FM magnetization as a function of time. The discrete Fourier transform of the Y component of $M_0 - M(t)$ yields the real and imaginary (absorption) part of the response of the system. All model calculations are evaluated at $T=300 \text{ K}$ with 64×64 elements. This size yields a system average good enough to be compared to experimental results.^{8,14}

IV. RESULTS AND DISCUSSION

In the CoFe/NiMn system, we estimate the average AF grain size (GS_{AF}) in the experimental sample by comparing the experimentally obtained HL to those obtained from model calculations with typical GS_{AF} values^{17,18} as observed in metallic systems. For $t_{\text{FM}}=20 \text{ nm}$ and $t_{\text{AF}}=50 \text{ nm}$ and using $GS_{\text{AF}}=40, 50, \text{ and } 60 \text{ nm}$ in the model calculations the values obtained are: $H_E=105, 115, \text{ and } 110 \text{ Oe}$; $H_{\text{EC}}=71, 50, \text{ and } 25 \text{ Oe}$, respectively; the experimental values are: $H_E=105 \text{ Oe}$ and $H_{\text{EC}}=40 \text{ Oe}$. A good agreement in both H_E and H_{EC} is obtained for $GS_{\text{AF}}=50 \text{ nm}$ and this value of GS_{AF} is retained in the evaluation of FMR response for a similar system. The HLs [Figs. 2(a) and 2(b)] and FMR responses [Figs. 2(c)] obtained from the model and experiment for $t_{\text{FM}}=20$ and 25 nm are presented. The ability of the model to predict experimental outcomes with this degree of accuracy is a point of merit especially in the light of absence of adjustable parameters. Table I summarizes the results for $t_{\text{FM}}=25, 20, 15, \text{ and } 10 \text{ nm}$. The model values (for f_R) exceed those of the experimental ones by 16% as t_{FM} is decreased to 10 nm. We attribute this to a possible change in the microstructure of the experimental sample, for example: the average AF grain size,¹⁹ effective grain volume of the FM and one-to-one correspondence between AF-FM grains. We repeat the model calculation for $t_{\text{FM}}=10 \text{ nm}$ with a bigger grain size of 70 nm. The results restore the numerical agreement of H_E and f_R to a certain extent between experimental and model outcomes. In the Py($t_{\text{FM}}=25 \text{ nm}$)/NiMn($t_{\text{AF}}=50 \text{ nm}$) system the model predicts f_R ranging from 2.9 to 5.3 GHz for a GS_{AF} variation of 70 to 25 nm, respectively. This brackets the experimentally observed value⁷ of 3.5 GHz. We now estimate the typical exchange field ($H_{\text{ex-AF}}$) experienced by an FM cell due to its coupling with the AF grain to examine the t_{FM} dependence of f_R . Using Eq. (1), we get

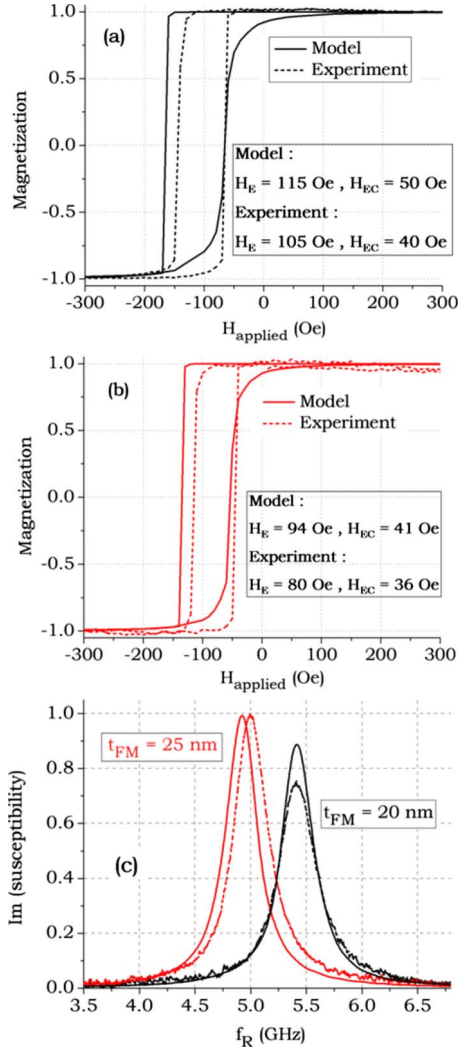


FIG. 2. (Color online) For the CoFe(t_{FM})/NiMn($t_{AF}=50$ nm) system: (a) HLs for $t_{FM}=20$ nm; (b) HLs for $t_{FM}=25$ nm; and (c) experimental (dashed lines) and model evaluated (solid lines) FMR response. There exists only one peak in the frequency range 0–10 GHz. The model plots are evaluated with $GS_{AF}=50$ nm.

$$H_{ex-AF} = \frac{J_{int}\tilde{N}}{M_S V_{FM}} \langle \hat{\mu}_{AF} \cdot \mathbf{X} \rangle, \quad (4)$$

where \mathbf{X} denotes the UA direction [Figs. 1(b) and 1(c)]. The $\langle \rangle$ brackets denote a time average as well as the ensemble average over the polycrystalline degrees of freedom of the AF, \tilde{N} is chosen to be $\sqrt{2N_{total}/\pi}$ where, $N_{total}=D_{lattice}GS_{AF}^2$. The system average UA field (H_{UA}) takes the form

$$H_{UA} = H_C + \frac{J_{int}\sqrt{2D_{lattice}/\pi}}{M_S GS_{AF}t_{FM}} \langle \hat{\mu}_{AF} \cdot \mathbf{X} \rangle, \quad (5)$$

where $H_C=2K_{FM}/M_S$. The Kittel equation for our film geometry is

$$f_R = (\gamma/2\pi)\sqrt{H_{UA}(H_{UA} + 4\pi M_S)}. \quad (6)$$

As $\langle \hat{\mu}_{AF} \cdot \mathbf{X} \rangle$ has no explicit t_{FM} dependence, its ensemble average ($\langle \hat{\mu}_{AF} \cdot \mathbf{X} \rangle_{EAV}$) is adequate to investigate f_R as a

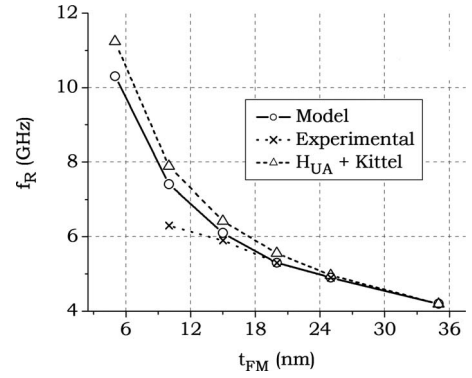


FIG. 3. f_R vs t_{FM} plots for CoFe/NiMn ($t_{AF}=50$ nm) system. The theoretical plots are evaluated with $GS_{AF}=50$ nm. Lines are a guide to the eye.

function of t_{FM} . Figure 3 shows three plots of f_R vs t_{FM} which were obtained: (1) experimentally, (2) from the model, and (3) using Eqs. (5) and (6) with parameter values: $GS_{AF}=50$ nm, $J_{int}=18 \times 10^{-14}$ ergs, $H_C=17.5$ Oe. To estimate $\langle \hat{\mu}_{AF} \cdot \mathbf{X} \rangle_{EAV}$, φ_Z is uniformly distributed in the range $[0, 2\pi]$, φ_X is chosen to be zero (without any loss of generality) and λ [Fig. 1(c)] is uniformly distributed in the range $[-\pi/4, \pi/4]$. For a quarter million averaging points, $\langle \hat{\mu}_{AF} \cdot \mathbf{X} \rangle_{EAV}$ yields 0.74. Experiments have demonstrated a similar trend.^{20,21} The deviation of the single domain particle prediction from the model prediction at low t_{FM} (Fig. 3) is not intuitively straightforward but can be loosely put as: for low t_{FM} , $\langle \hat{\mu}_{AF} \cdot \mathbf{X} \rangle_{EAV}$ decreases with the finiteness of $A_{exchange}$.

The model evaluated f_R vs t_{AF} plot is shown in Fig. 4(a). We will discuss below the case: $GS_{AF}=50$ nm as a similar discussion holds for $GS_{AF}=30$ nm. A decrease in t_{AF} below 45 nm increases the population of the AF grains satisfying the condition: $K_{AF}V_{AF} \ll 4J_{int}\tilde{N}$. Such grains are devoid of energy barriers [Eq. (2)] thereby turning superparamagnetic. These grains readily trail (align with) the FM moments responding to the rf field. Their inability to consolidate the UA direction results in the reduction in H_{UA} . An increase in t_{AF} from 45 to 75 nm stabilizes the AF grains and pins them in their field-cooling configuration resulting in an increase in H_{UA} . This increase reaches a maximum value denoting an optimum number of AF grains consolidating the UA direc-

TABLE I. Exchange bias (H_E), enhanced coercivity (H_{EC}), and resonance frequency (f_R) obtained from experiments (exp.) and model calculations for CoFe(t_{FM})/NiMn($t_{AF}=50$ nm). Model calculations are done with $GS_{AF}=50$ nm. (* denotes the model calculations with $GS_{AF}=70$ nm.)

t_{FM} (nm)	H_E (model) (Oe)	H_E (exp.) (Oe)	H_{EC} (model) (Oe)	H_{EC} (exp.) (Oe)	f_R (model) (GHz)	f_R (exp.) (GHz)
25	94	80	41	36	4.9	5.0
20	115	105	50	40	5.4	5.4
15	148	119	59	39	6.2	5.9
10	226 190*	140	78 23*	56	7.4 6.0*	6.4

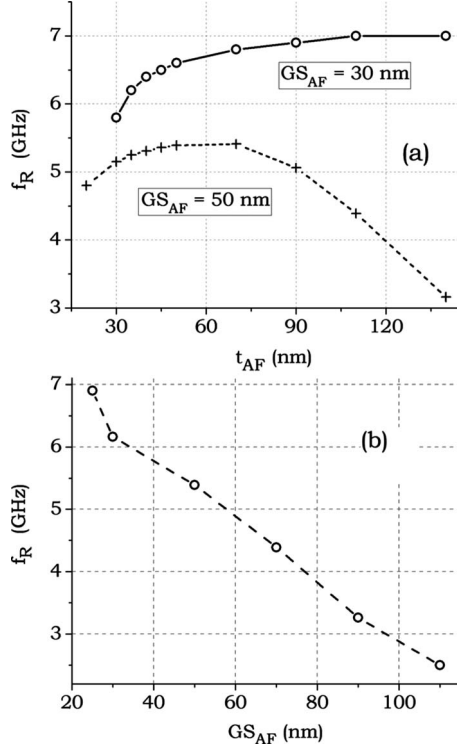


FIG. 4. Model evaluated: (a) f_R vs t_{AF} for CoFe ($t_{FM}=20$ nm)/NiMn with $GS_{AF}=30$ nm (open circle symbols), 50 nm [(+) symbols] and (b) f_R vs GS_{AF} for CoFe ($t_{FM}=20$ nm)/NiMn ($t_{AF}=50$ nm). Lines are a guide to the eye.

tion. Beyond this maximum ($t_{AF} > 75$ nm), a further increase in t_{AF} results in an additional number of AF grains attaining thermal stability but the net angular dispersion in $\hat{\mu}_{AF}$ reduce H_{UA} . This reduction in H_{UA} is mainly dictated by the magnetic structure of the AF $\langle \hat{\mu}_{AF} \cdot \mathbf{X} \rangle_{EAV}$. A similar trend of f_R vs t_{AF} has also been experimentally observed.^{4,22} Next we discuss the GS_{AF} dependence of f_R [Fig. 4(b)]. An increase in GS_{AF} enhances the locking of the AF grains along the UA

direction [Eq. (2)] simultaneously decreasing the UA field [Eq. (5)]. The net effect of these two conflicting contributions is a monotonic decrease in f_R as a function of GS_{AF} [Fig. 4(b)]. This implies that $(J_{int} \sqrt{2D_{lattice}} / \pi / M_S GS_{AF} t_{FM})$ has a dominant contribution over $\langle \hat{\mu}_{AF} \cdot \mathbf{X} \rangle$ in the case of FMR measurements. The nontrivial behaviors of f_R vs t_{AF} and f_R vs GS_{AF} attributable to the thermal activation of the large AF degree of freedom have not been the natural outcome of any previous theoretical work. To estimate the (theoretical) maximum f_R of any particular system from HLs, we (model) compute HLs at $T=0$ K and measure the field (H_{SW}) at which the FM magnetization reverses starting from the field-cooled state. For the CoFe($t_{FM}=20$ nm)/NiMn($t_{AF}=50$ nm) system with $GS_{AF}=50$ nm, H_{SW} is 155 Oe which corresponds to a f_R value of 5.3 GHz using $H_{UA}=H_{SW}$ in Eq. (6). This fits well with the values obtained from both the model and the experiment [Fig. 4(a)].

V. CONCLUSIONS

We have established the tunability of f_R by altering thermal stability of the AF (dictated by t_{AF} and GS_{AF}) in an AF/FM system. As the UAs measured by H_E and f_R have different physical origin, a general formula may not be achievable to predict f_R based on information from experimental HLs for a wide range of either t_{AF} or GS_{AF} or temperature. Nevertheless, the maximum attainable f_R in such a system can be estimated from a (experimental) HL evaluated at a temperature (low enough) such that the coercivity of the system is mainly due to the magnetocrystalline anisotropy of the FM.

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